

# Department of Automotive Technologies – Vehicle Mechanics Fundamentals

**Gábor Sipos**



Lecture 3

# Basic information

Week nr.	Date		Lecture (Monday)		Lab (date+1;Tuesday)
1	12th Feb	1	General information, Tyre, Driving force	1	Lab
2	19th Feb	2	Longitudinal and lateral behaviour		
3	26th Feb	3	Concepts and over/understeer	2	Lab
4	4th Mar	4	Weight transfer		
5	11th Mar	5	Bicycle model	3	Lab
6	18th Mar	T1	Midterm exam I. ONLINE		
7	25th Mar	6	Braking and brakes ONLINE	4	Lab ONLINE
8	1st Apr	-	Break		
9	8th Apr	7	Systems of the vehicle	T1 R	Exam 1 - subsequent
10	15th Apr	8	Quarter vehicle model ONLINE		
11	22nd Apr		Break		Break
12	29th Apr	T2	Midterm exam II. ONLINE		
13	6th May	9	Tyre management	T2 R	Exam 2 - subsequent
14	13th May	10	Racecar engineering		

# Note



- Please do not consider operative information from online lecture, it's an older record.
- Bring laptop to lab course!

What kind of car part can you see on the picture?



- A. 1-upright 2-rim, 3-wheel bearing, 4-tyre, 5- wheel nuts, 6-wheel stud
- B. 1-upright 2-rim, 3-wheel, 4-tyre, 5- wheel studs, 6-brake caliper
- C. 1-wheel hub 2-rim, 3-wheel bearing, 4-tyre, 5- wheel studs, 6-brake caliper
- D. 1-wheel hub 2-rim, 3-wheel bearing, 4-tyre, 5- wheel nuts, 6-upright

What kind of car part can you see on the picture?



- A. 1-upright 2-rim, 3-wheel bearing, 4-tyre, 5- wheel studs, 6-wheel stud
- B. 1-upright 2-rim, 3-wheel, 4-tyre, 5- wheel studs, 6-brake caliper
- C. 1-wheel hub 2-rim, 3-wheel bearing, 4-tyre, 5- wheel studs, 6-brake caliper
- D. **1-wheel hub 2-rim, 3-wheel bearing, 4-tyre, 5- wheel nuts, 6-upright**

# Quiz

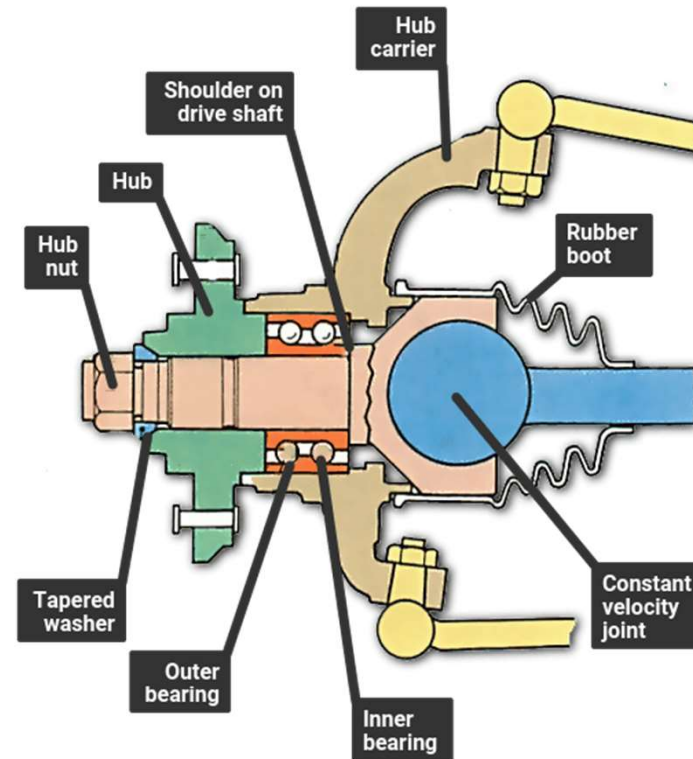
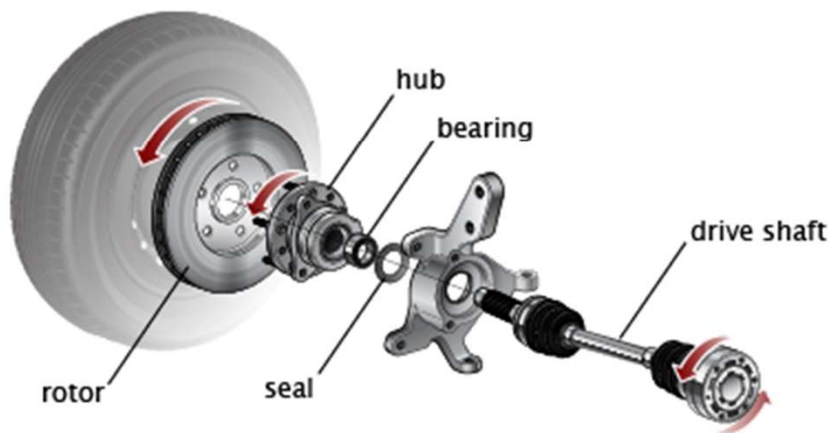
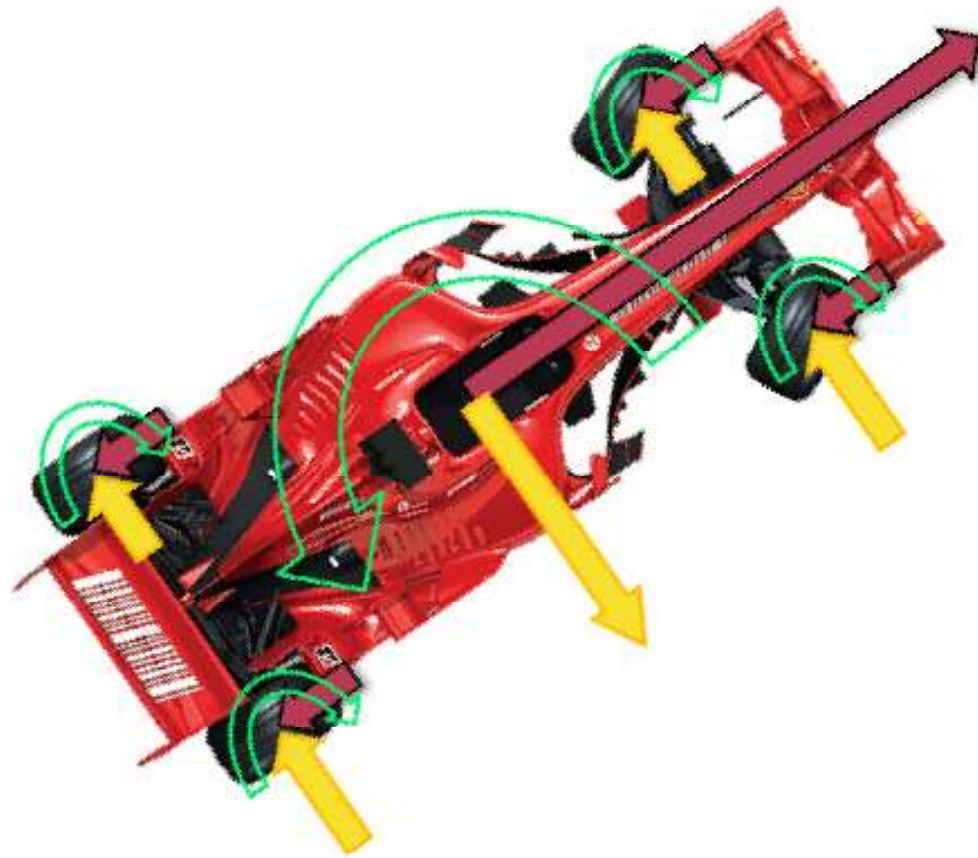
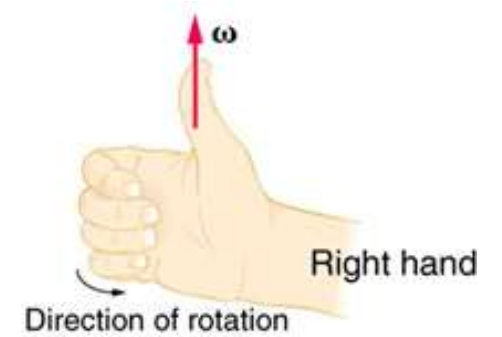
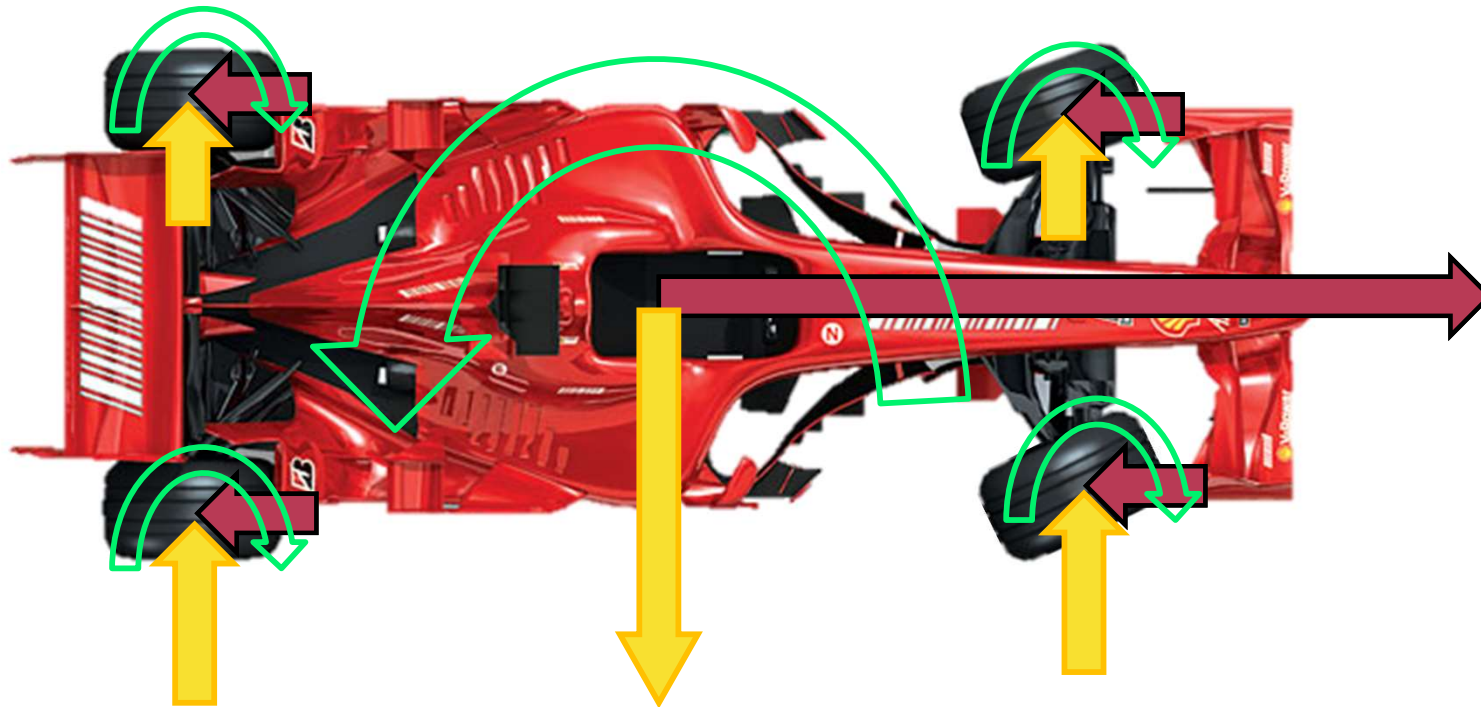


Image courtesy of ClearMechanic.com

# Vehicle dynamics fundamentals

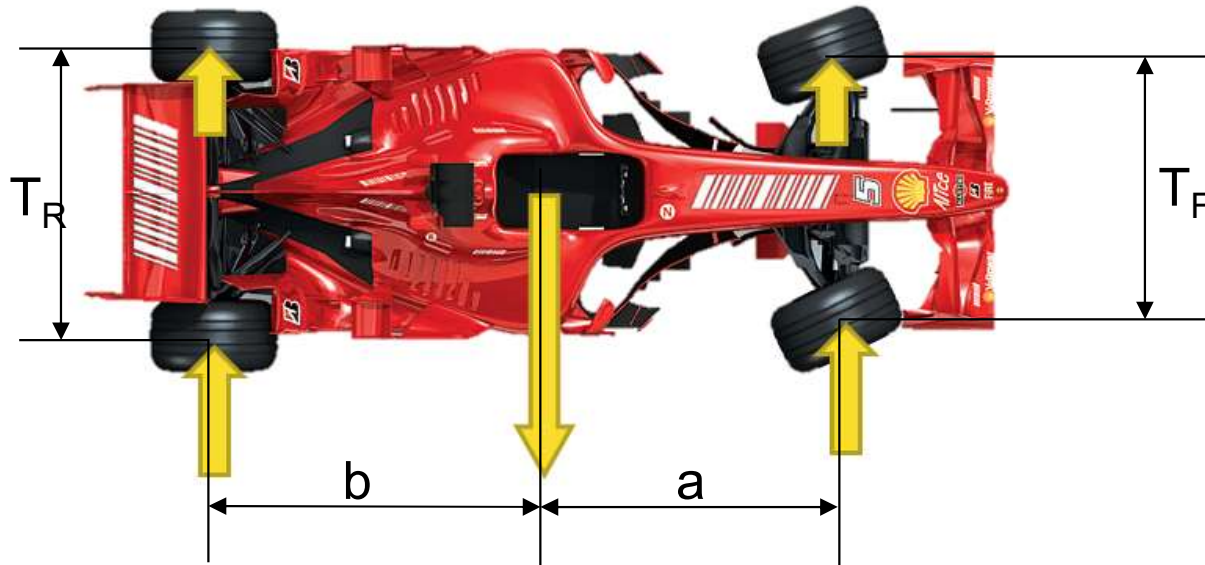


# Vehicle dynamics fundamentals





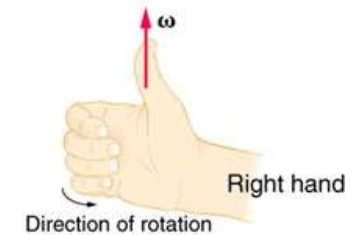
## Steady State Basics



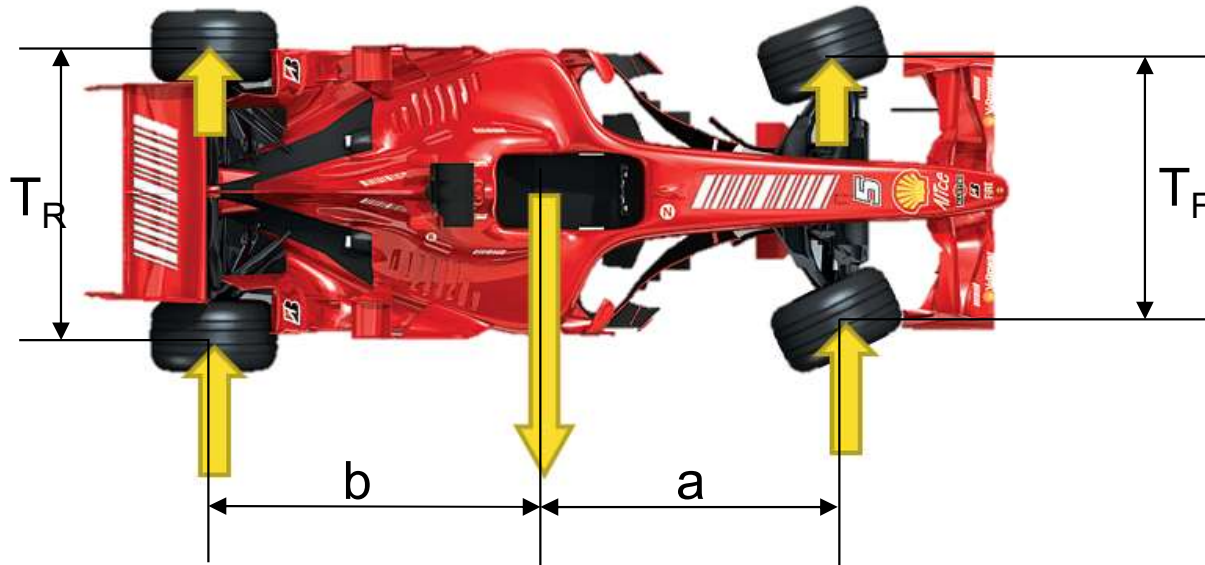
$$\sum F_y \rightarrow F_{y_{FL}} + F_{y_{FR}} + F_{y_{RL}} + F_{y_{RR}} = \text{Mass} \cdot \text{Lateral Acc}$$

$$(F_{y_{FL}} + F_{y_{FR}} + F_{y_{RL}} + F_{y_{RR}}) / \text{Mass} = \text{Lateral Acc}$$

$$\sum M = 0 \rightarrow (F_{y_{FL}} + F_{y_{FR}}) \cdot a - (F_{y_{RL}} + F_{y_{RR}}) \cdot b = 0$$

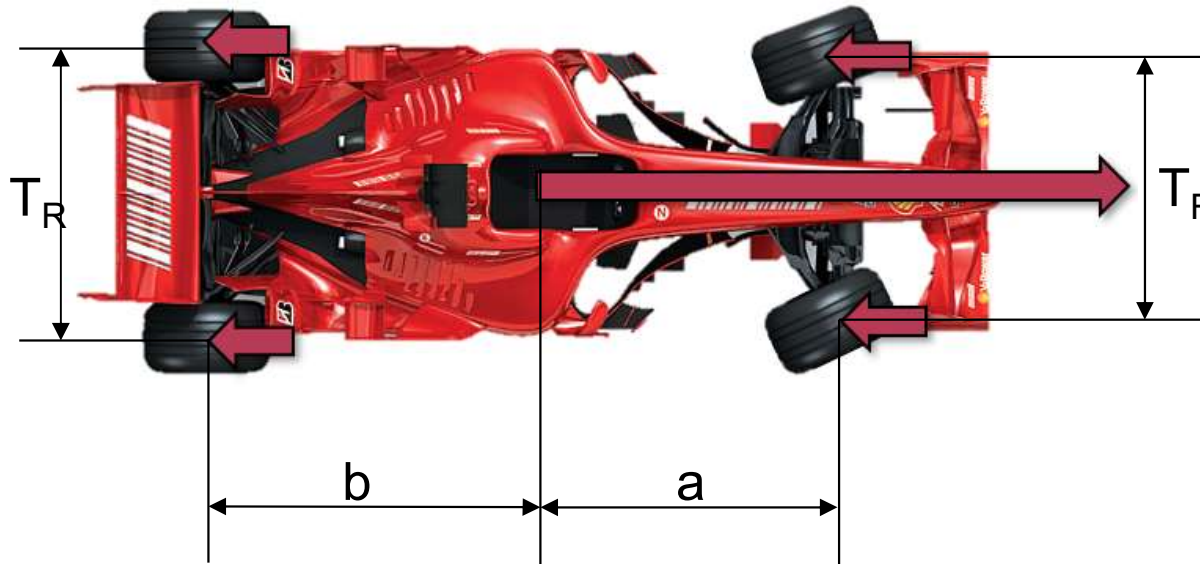


## Steady State Basics



$$A_f = A_r$$
$$(F_{y_{FL}} + F_{y_{FR}})/m_F = (F_{y_{RL}} + F_{y_{RR}})/m_R$$

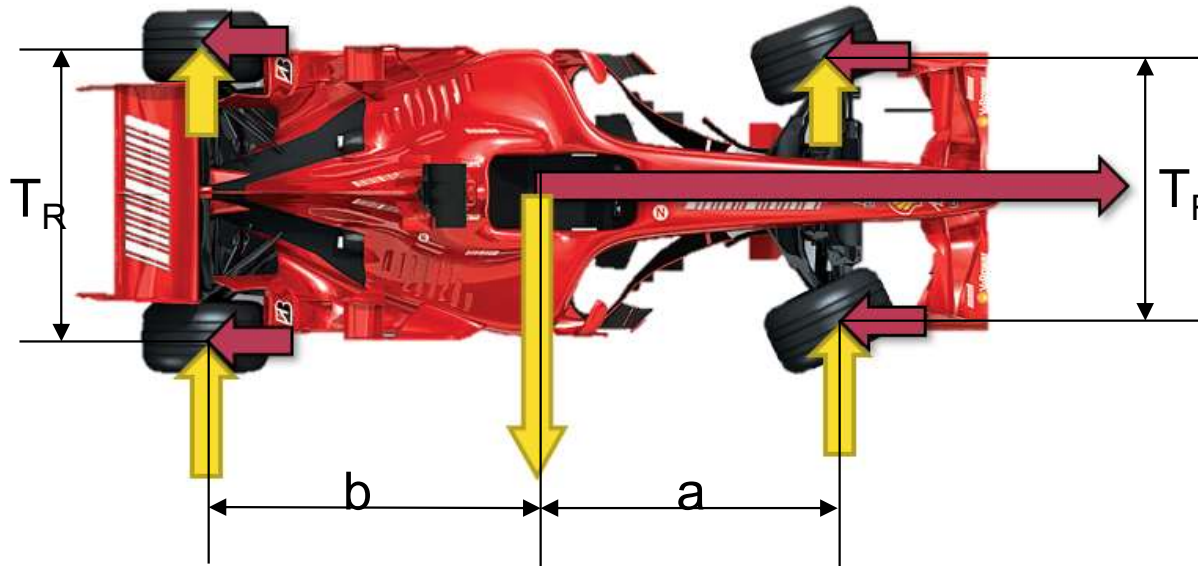
## Steady State Basics



$$\sum F_x \rightarrow F_{xFL} + F_{xFR} + F_{xRL} + F_{xRR} = \text{Mass} \cdot \text{Longitudinal Acc}$$

$$\sum M = 0 \rightarrow \left( F_{xFR} \cdot \frac{T_F}{2} + F_{xRR} \cdot \frac{T_R}{2} \right) - \left( F_{xFL} \cdot \frac{T_F}{2} + F_{xRL} \cdot \frac{T_R}{2} \right) = 0$$

## Steady State Basics

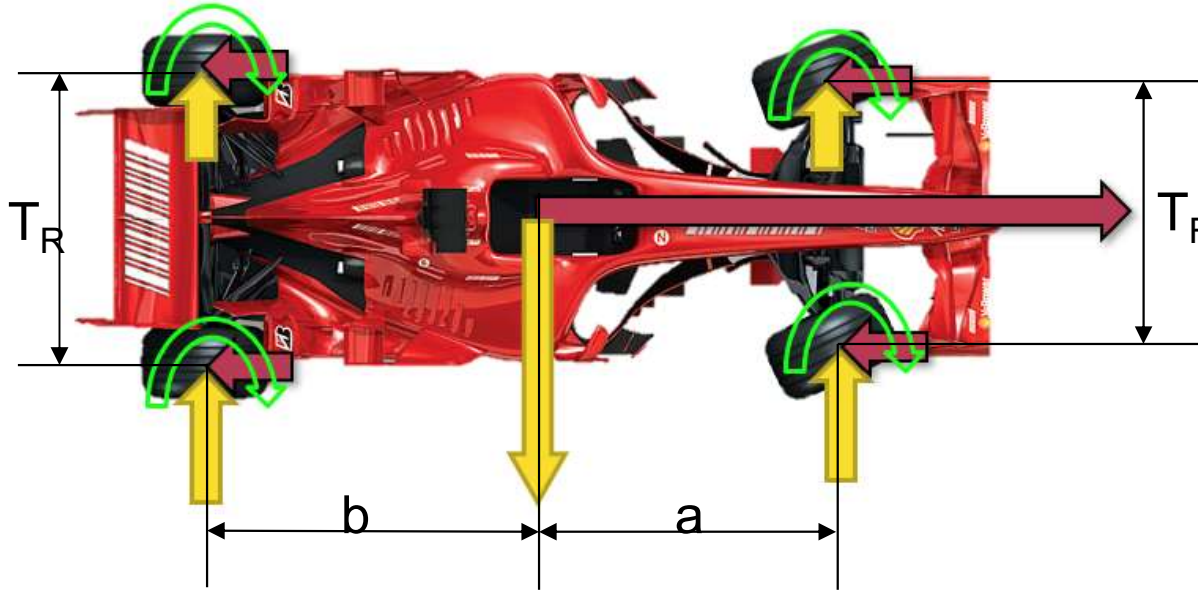


$$\sum F_y \rightarrow F_{y_{FL}} + F_{y_{FR}} + F_{y_{RL}} + F_{y_{RR}} = \text{Mass} \cdot \text{Lateral Acc}$$

$$\sum F_x \rightarrow F_{x_{FL}} + F_{x_{FR}} + F_{x_{RL}} + F_{x_{RR}} = \text{Mass} \cdot \text{Longitudinal Acc}$$

$$\sum M = 0 \rightarrow [(F_{y_{FL}} + F_{y_{FR}}) \cdot a - (F_{y_{RL}} + F_{y_{RR}}) \cdot b] + [(F_{x_{FR}} \cdot \frac{T_F}{2} + F_{x_{RR}} \cdot \frac{T_R}{2}) - (F_{x_{FL}} \cdot \frac{T_F}{2} + F_{x_{RL}} \cdot \frac{T_R}{2})] = 0$$

## Steady State Basics



$$\sum F_y \rightarrow F_{y_{FL}} + F_{y_{FR}} + F_{y_{RL}} + F_{y_{RR}} = \text{Mass} \cdot \text{Lateral Acc}$$

$$\sum F_x \rightarrow F_{x_{FL}} + F_{x_{FR}} + F_{x_{RL}} + F_{x_{RR}} = \text{Mass} \cdot \text{Longitudinal Acc}$$

$$\sum M = 0 \rightarrow [(F_{y_{FL}} + F_{y_{FR}}) \cdot a - (F_{y_{RL}} + F_{y_{RR}}) \cdot b] + [(F_{x_{FR}} \cdot \frac{T_F}{2} + F_{x_{RR}} \cdot \frac{T_R}{2}) - (F_{x_{FL}} \cdot \frac{T_F}{2} + F_{x_{RL}} \cdot \frac{T_R}{2})] - M_{z_{FL}} - M_{z_{FR}} - M_{z_{RL}} - M_{z_{RR}} = 0$$

## Steady State Basics - SkidPad



## Steady State Basics

$$V_x = \dot{\theta} R \quad LatG = \frac{v^2}{R}$$

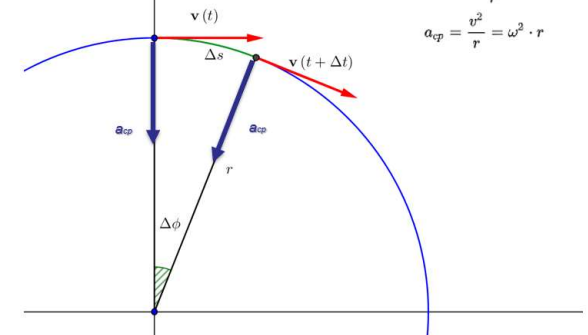
$$LatG = \frac{\dot{\theta} v^2}{v}$$

$$\dot{\theta} = \frac{LatG}{v_x}$$

### Lateral dynamics - steady state condition

Centripetal force and acceleration

$$F_C = \frac{m \cdot v^2}{r}$$
$$a_{cp} = \frac{v^2}{r} = \omega^2 \cdot r$$



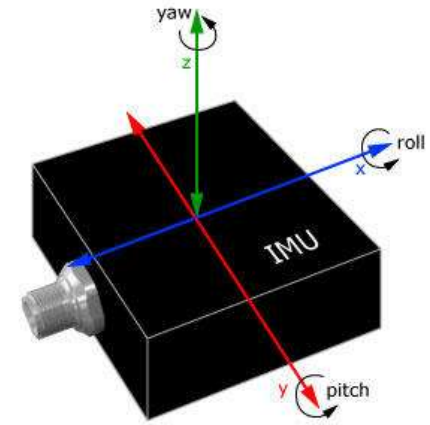
## Steady State Basics

$$V_x = \dot{\theta} R \quad LatG = \frac{v^2}{R}$$

$$LatG = \frac{\dot{\theta} v^2}{v}$$

$$\dot{\theta} = \frac{LatG}{v_x}$$

→ latG sensor  
 → speed sensor (~r<sub>dyn</sub> ?)  
 → yaw rate sensor



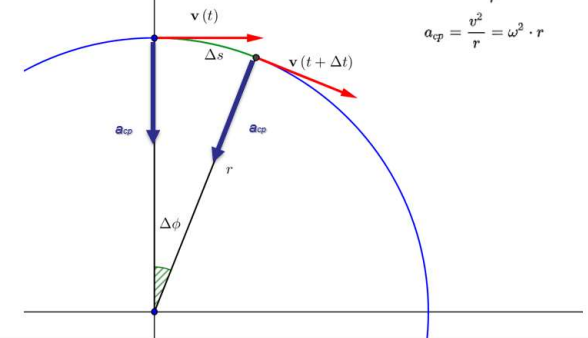
### Lateral dynamics - steady state condition



Centripetal force and acceleration

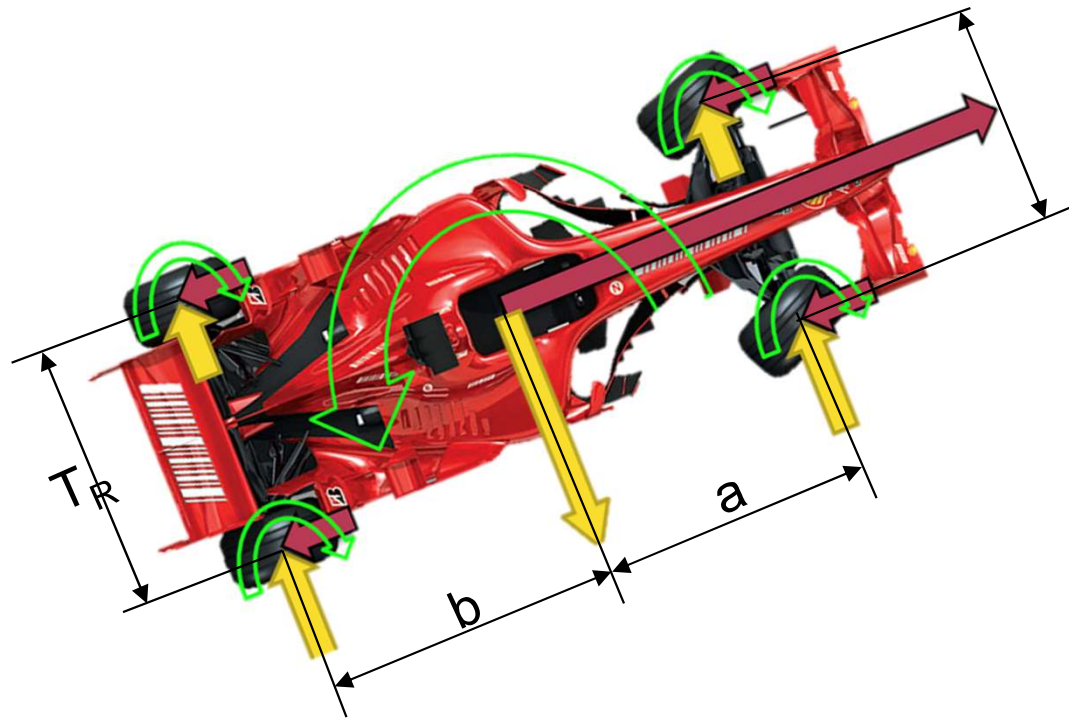
$$F_C = \frac{m \cdot v^2}{r}$$

$$a_{cp} = \frac{v^2}{r} = \omega^2 \cdot r$$





## Transient Basics: Yaw Moment Equation



$I_{ZZ}$  : moment of inertia [ $kgm^2$ ]

$d^2\theta/dt^2$  : Yaw acceleration  
: d(yaw rate)/dt  
: d(gyro)/dt

$$\sum M \rightarrow [(F_{yFL} + F_{yFR}) \cdot a - (F_{yRL} + F_{yRR}) \cdot b] + [(F_{xFR} \cdot \frac{T_F}{2} + F_{xRR} \cdot \frac{T_R}{2}) - (F_{xFL} \cdot \frac{T_F}{2} + F_{xRL} \cdot \frac{T_R}{2})] - M_{zFL} - M_{zFR} - M_{zRL} - M_{zRR} = I_{ZZ} \cdot d^2 \theta / dt^2$$

# E-Car design

Where to place the last module of the newly designed battery for RWD car?



# E-Car design

Where to place the last module of the newly designed battery for RWD car?

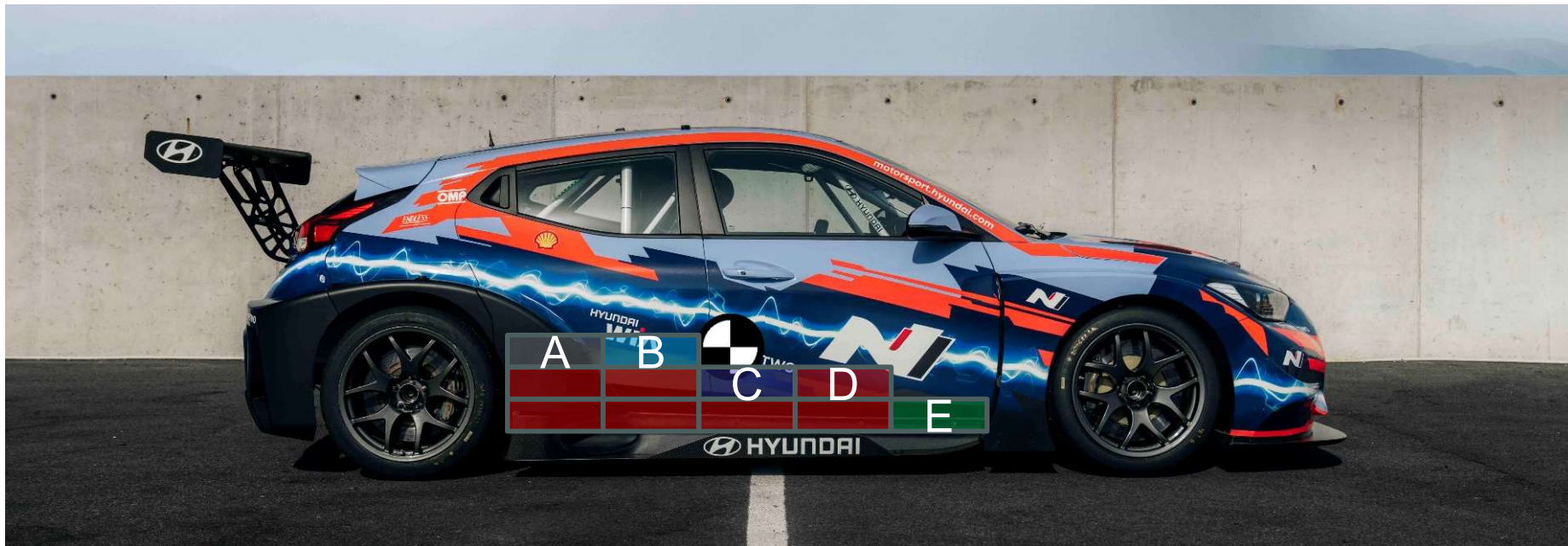
A – suggest to improve standing starts

B – suggest to improve standing starts & keep inertia low

C – suggest to keep inertia low, good compromise for CoG

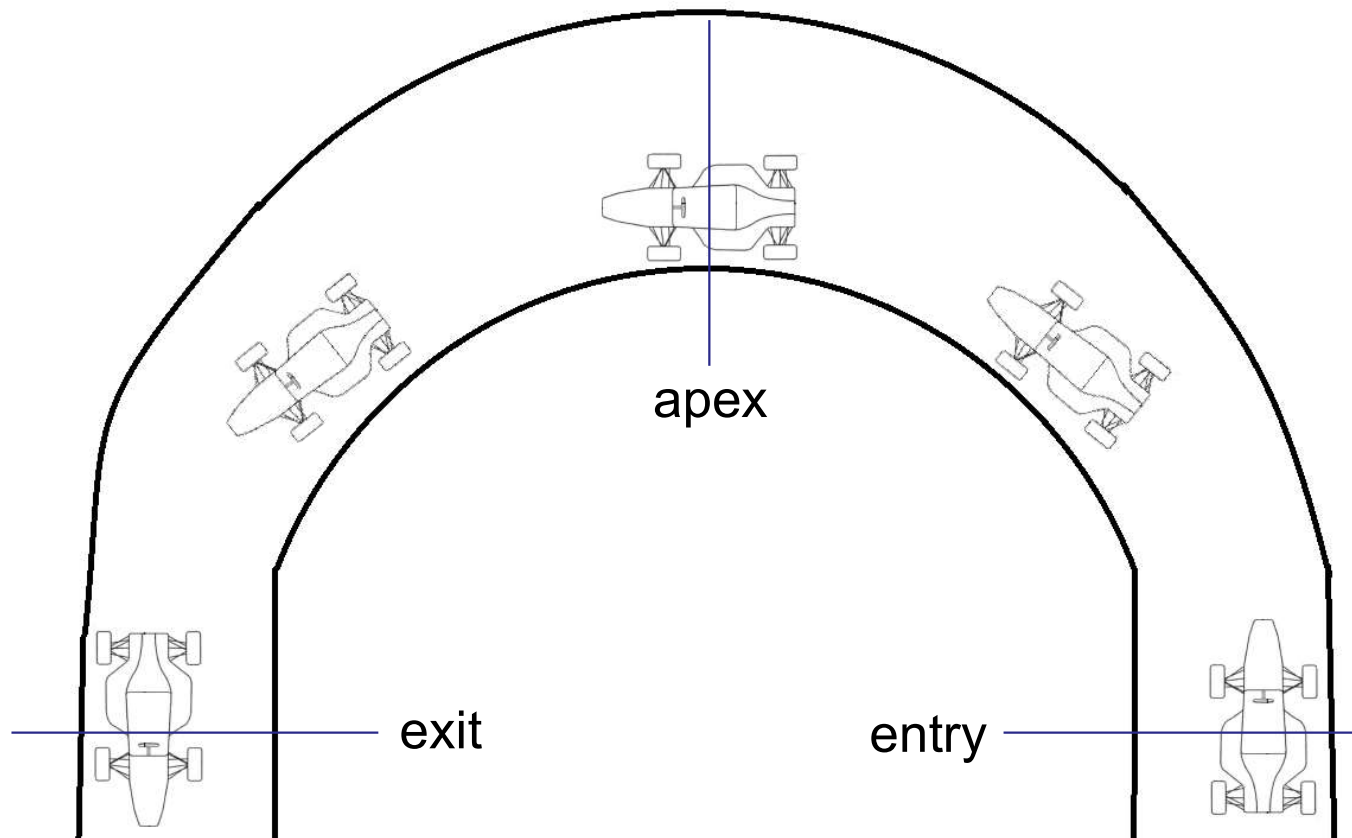
D – suggest for lowest inertia and best option for CoG

E – suggest lowest CoG and good improvement of inertia



# Analysis: 180° turn

,to use yaw moment'

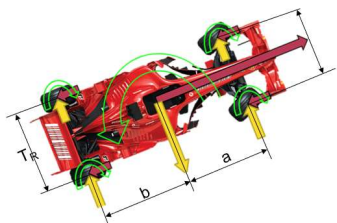


## Conclusions

- To be 'red car' we need more yaw velocity in less time -> greater yaw acceleration -> which means more yaw moment. Positive at corner entry and negative at corner exit. As a conclusion, more relative **front grip** at corner entry and more relative **rear grip** at corner exit required for the red car.

**Vehicle dynamics fundamentals**

Transient Basics: Yaw Moment Equation



$I_{ZZ}$  : moment of inertia [ $kgm^2$ ]

$d^2\theta/dt^2$  : Yaw acceleration  
: d(yaw rate)/dt  
: d(gyro)/dt

$$\sum M \rightarrow [(F_{yFL} + F_{yFR}) \cdot a - (F_{yRL} + F_{yRR}) \cdot b] + [(F_{xFR} \cdot \frac{T_F}{2} + F_{xRR} \cdot \frac{T_R}{2}) - (F_{xFL} \cdot \frac{T_F}{2} + F_{xRL} \cdot \frac{T_R}{2})]$$

$$-M_{zFL} - M_{zFR} - M_{zRL} - M_{zRR} = I_{ZZ} \cdot d^2 \theta / dt^2$$



$$\sum M \rightarrow [(F_{yFL} + F_{yFR}) \cdot a - (F_{yRL} + F_{yRR}) \cdot b] + [(F_{xFR} \cdot \frac{T_F}{2} + F_{xRR} \cdot \frac{T_R}{2}) - (F_{xFL} \cdot \frac{T_F}{2} + F_{xRL} \cdot \frac{T_R}{2})]$$

$$-M_{zFL} - M_{zFR} - M_{zRL} - M_{zRR} = I_{ZZ} \cdot d^2 \theta / dt^2$$

## Conclusions - example

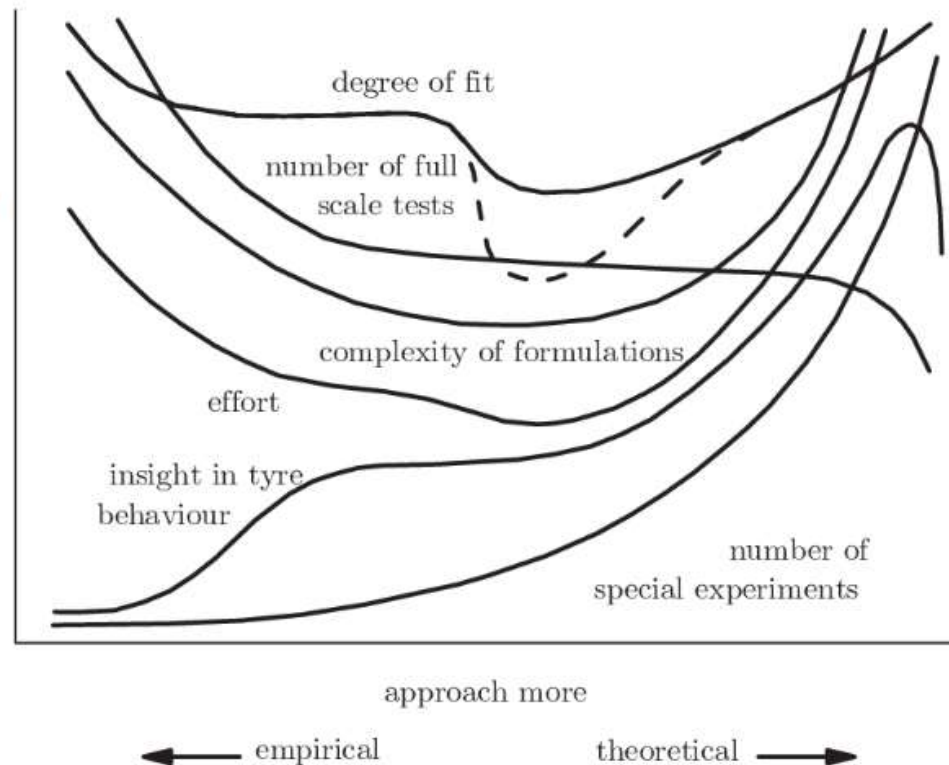
$$\left[ \begin{array}{c} \text{entry} \\ \left( F_{y_{FL}} + F_{y_{FR}} \right) \cdot a - \left( F_{y_{RL}} + F_{y_{RR}} \right) \cdot b \\ +3\% \qquad \qquad \qquad +2\% \end{array} \right]$$

$$\left[ \begin{array}{c} \text{apex} \\ \left( F_{y_{FL}} + F_{y_{FR}} \right) \cdot a - \left( F_{y_{RL}} + F_{y_{RR}} \right) \cdot b \\ +4\% \qquad \qquad \qquad +4\% \end{array} \right]$$

$$\left[ \begin{array}{c} \text{exit} \\ \left( F_{y_{FL}} + F_{y_{FR}} \right) \cdot a - \left( F_{y_{RL}} + F_{y_{RR}} \right) \cdot b \\ +2\% \qquad \qquad \qquad +3\% \end{array} \right]$$

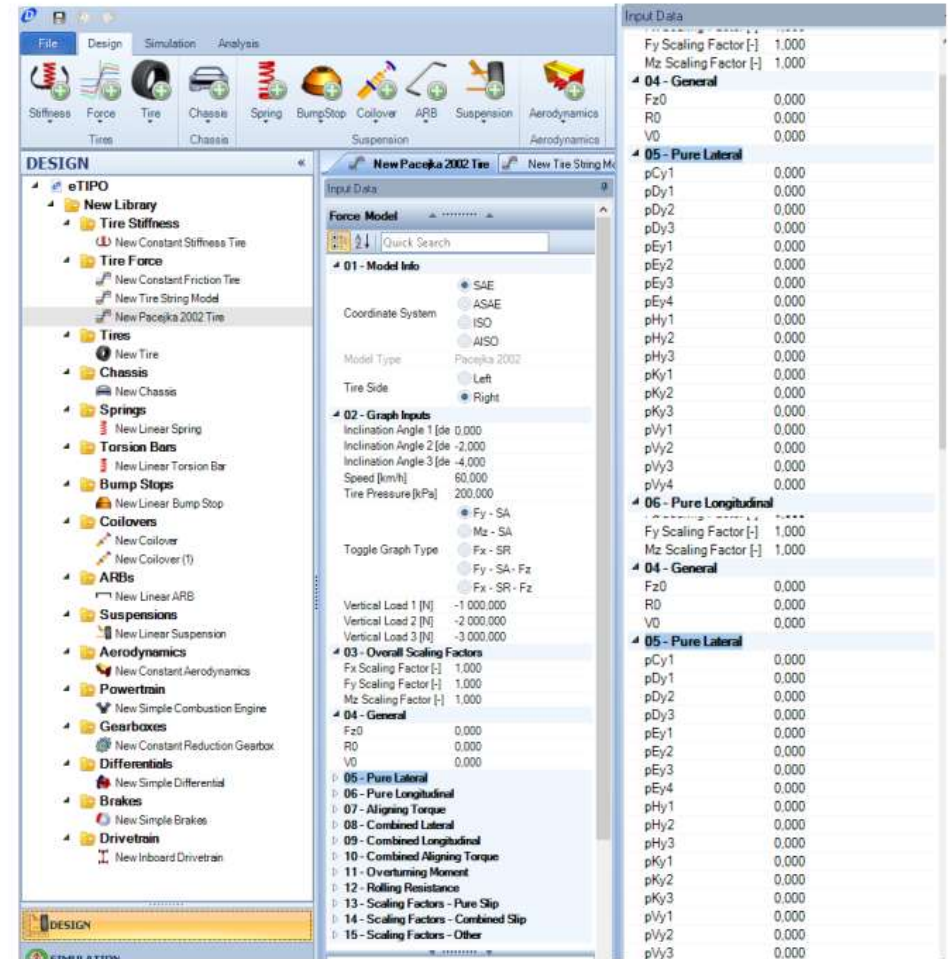
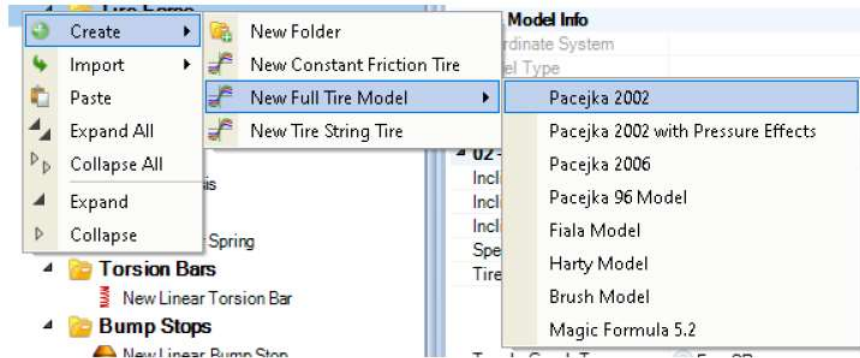
# Tyre model

from experimental data only	using similarity method	through simple physical model	through complex physical model
fitting full scale tyre test data by regression techniques	distorting, rescaling and combining basic characteristics	using simple mechanical representation, possibly closed form solution	describing tyre in greater detail, computer simulation, finite element method
e.g. <i>Magic Formula</i>		e.g. <i>Brush model</i>	e.g. <i>RMOD-K, FTire</i>



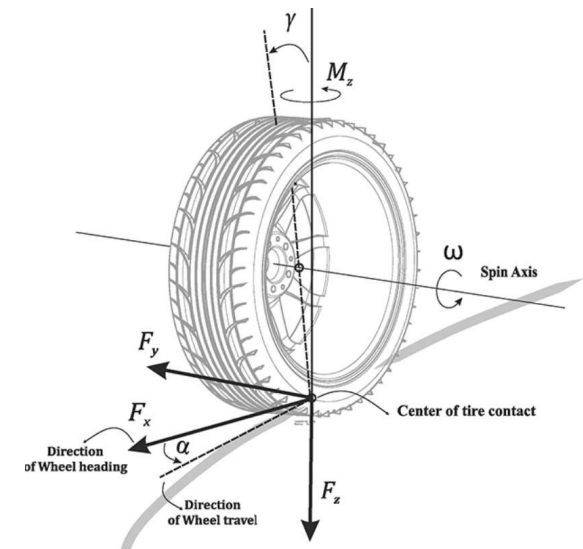
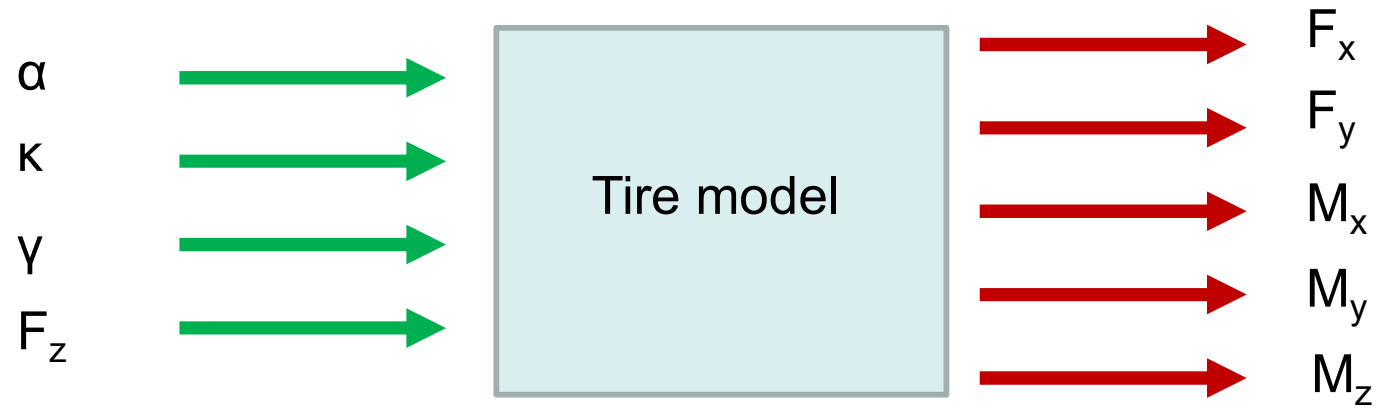
2: Classification of tire models according to H.B.Pacejka

# Tyre model

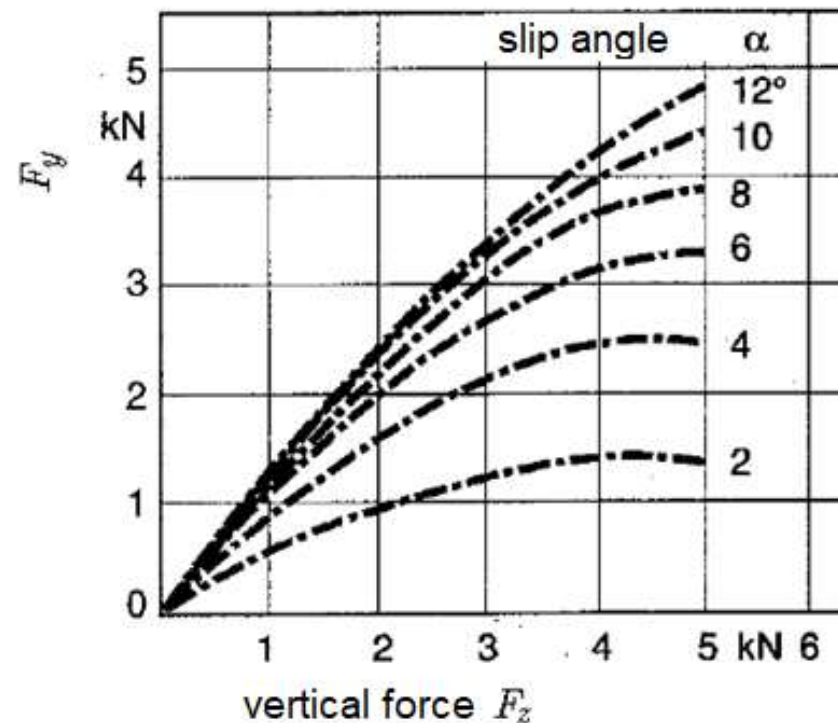
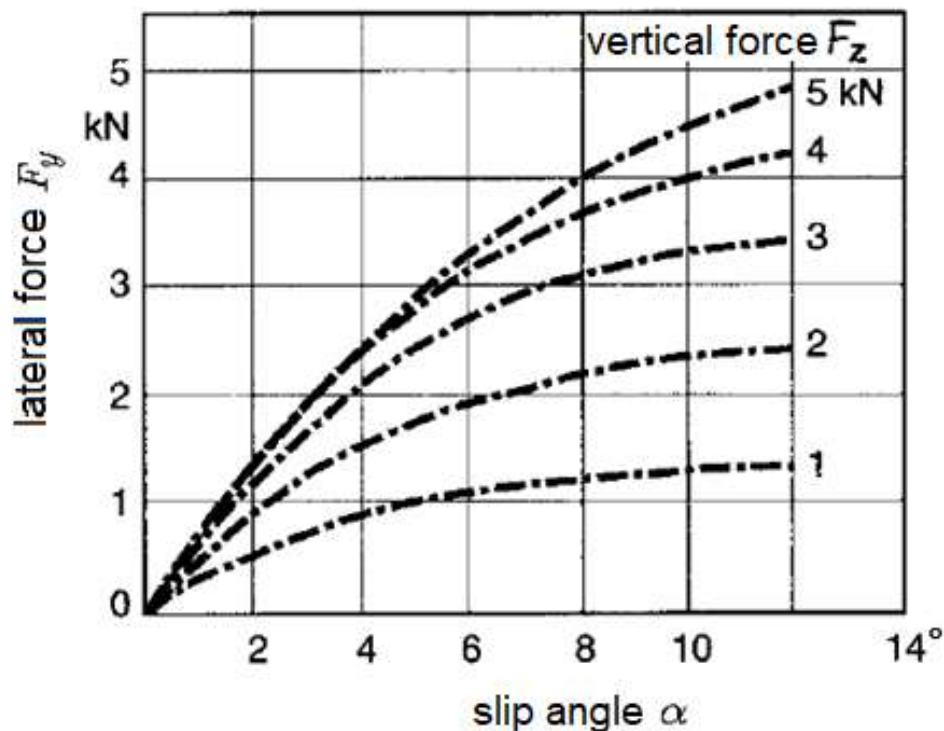




# Tyre model



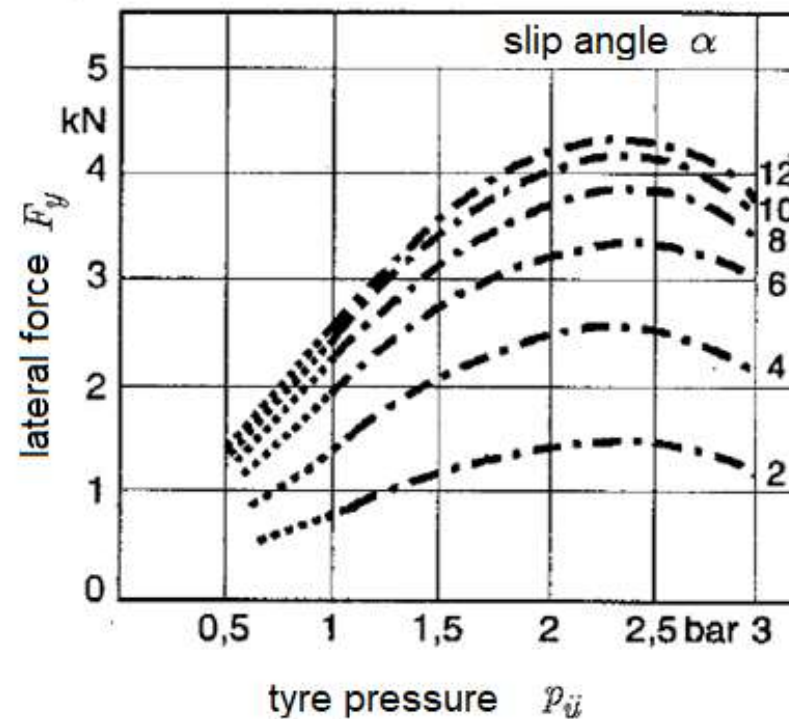
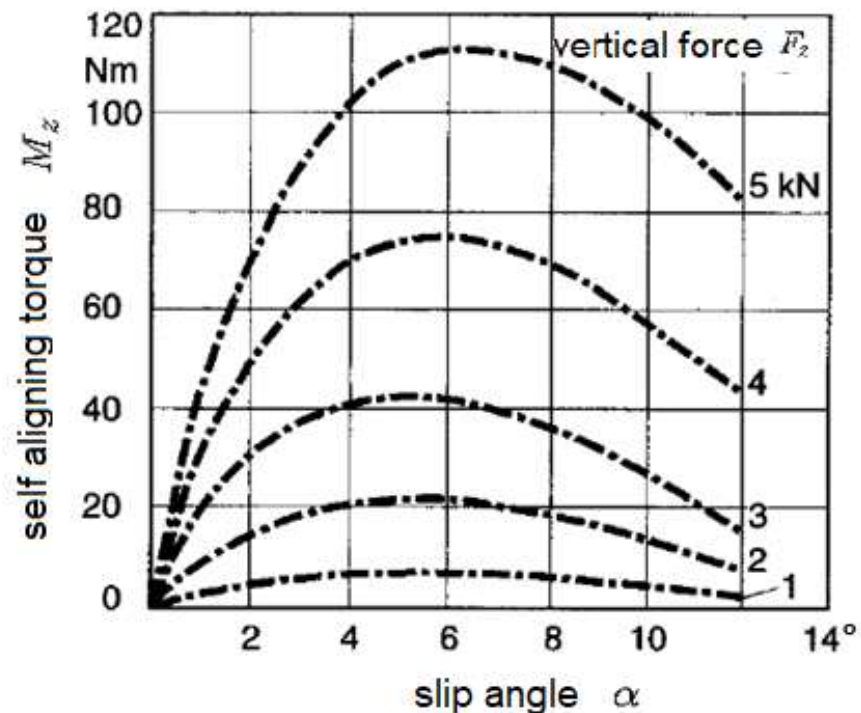
# Vertical load, lateral force and slip angle diagrams



tyre 175 HR 14  
 5 Jx14  
 tread depth 9 mm  
 vehicle speed 14 m/s  
 tyre pressure 1,8 bar

Quelle: Wallentowitz 1997

# Vertical load, lateral force and slip angle diagrams



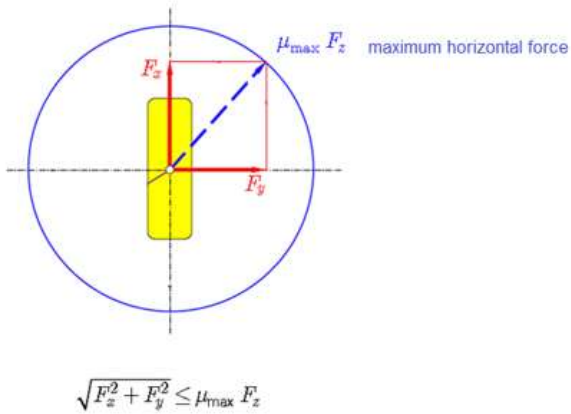
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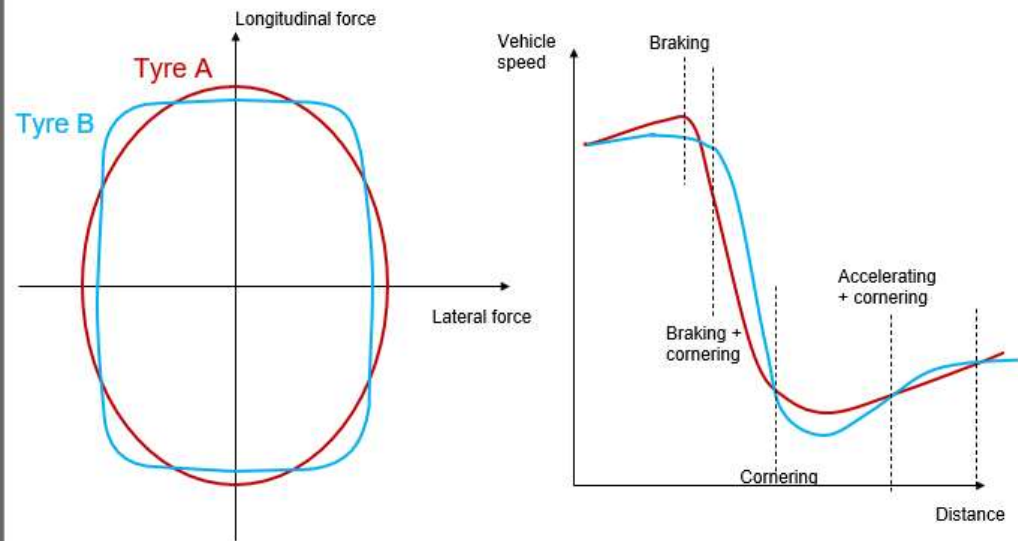
## Conclusions - example

### Kamm circle

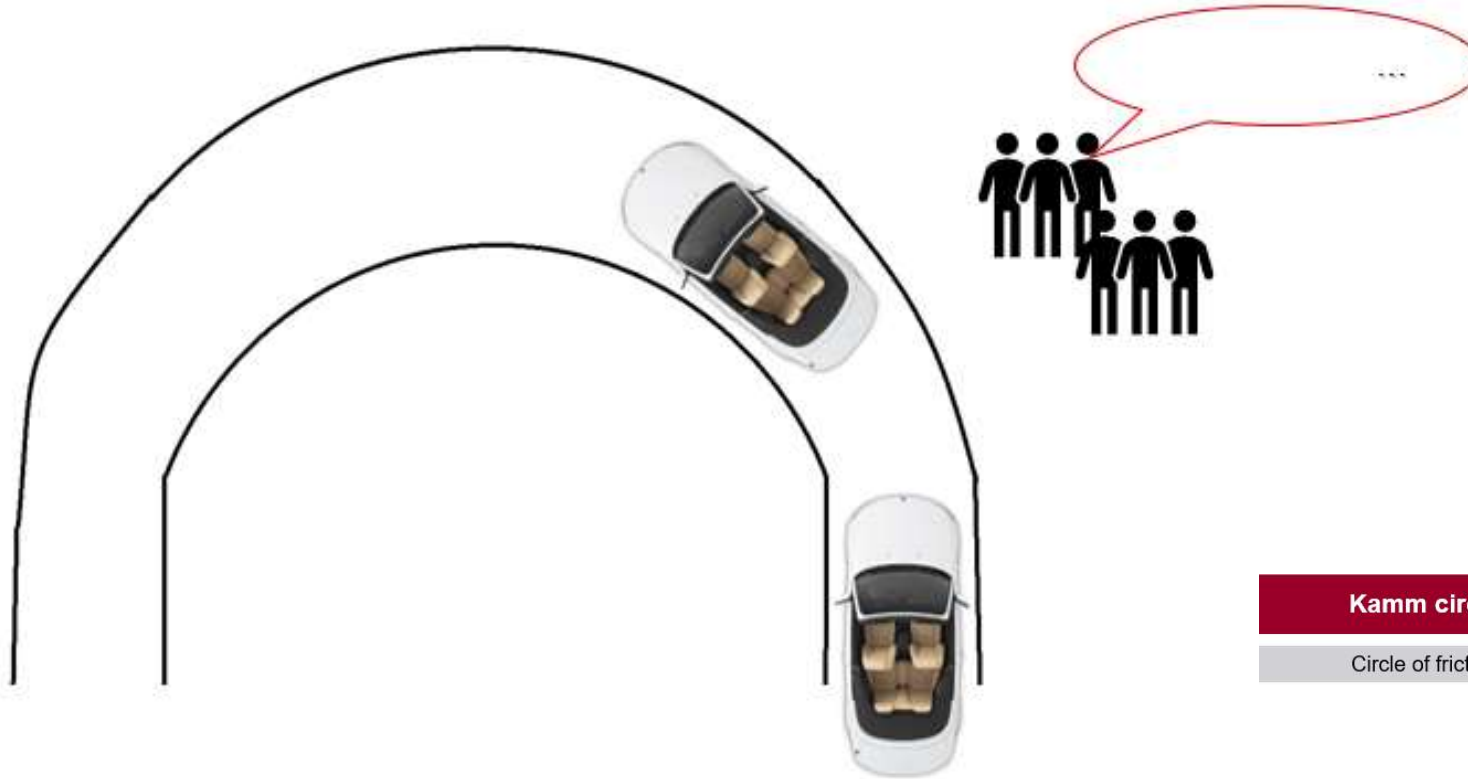
Circle of friction



### Different tires

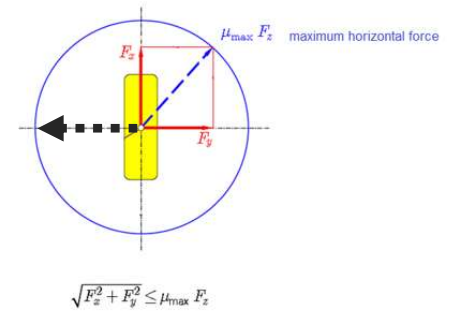


## BMW

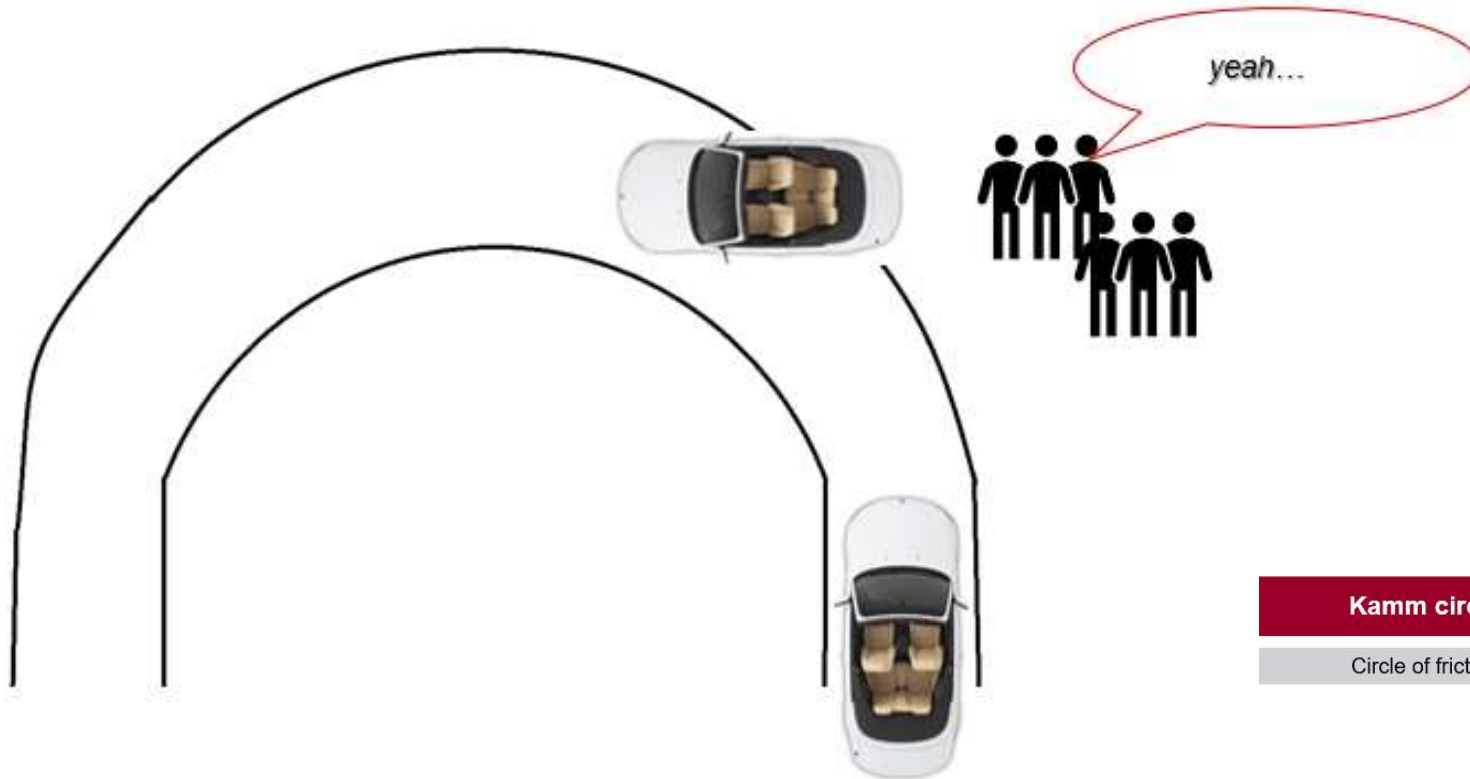


### Kamm circle

Circle of friction

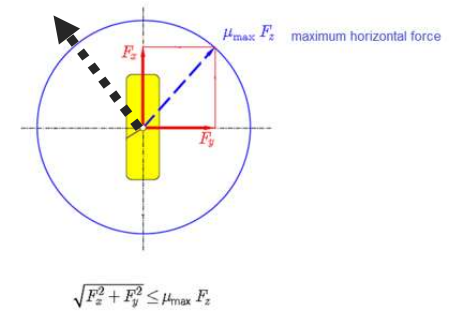


## BMW

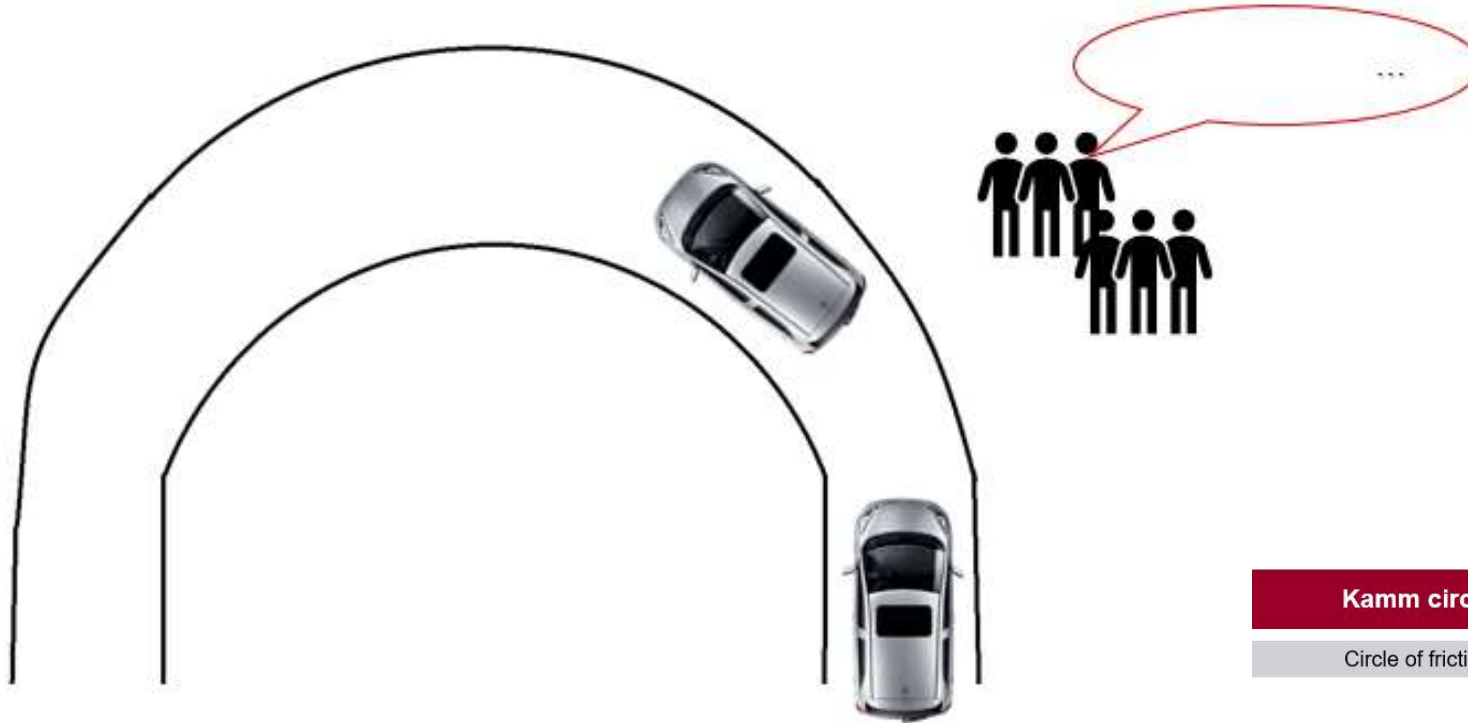


### Kamm circle

Circle of friction

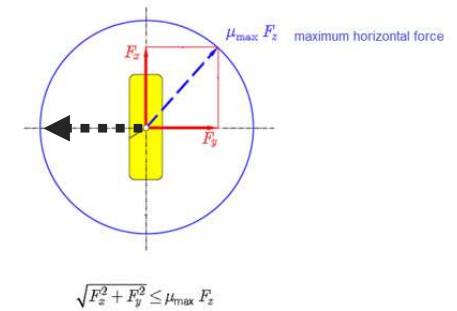


## KIA

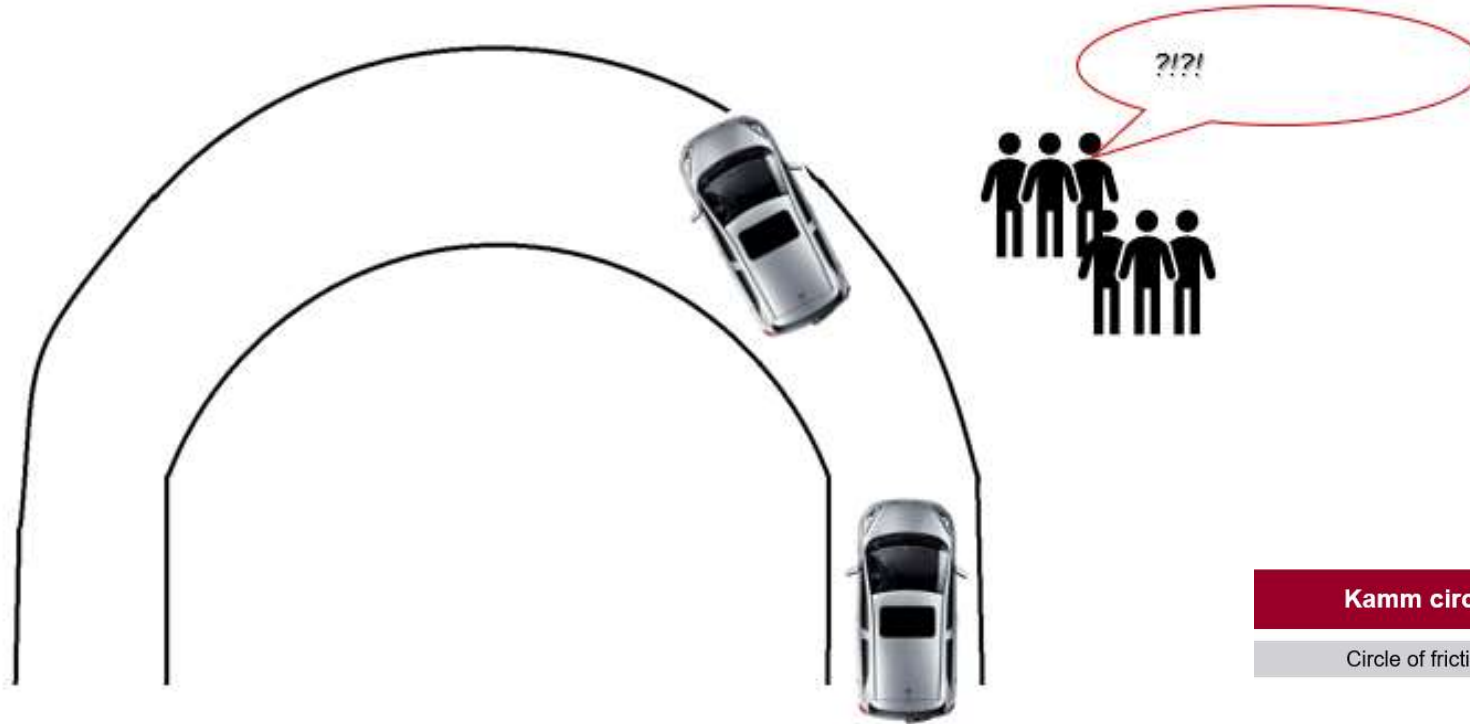


### Kamm circle

Circle of friction

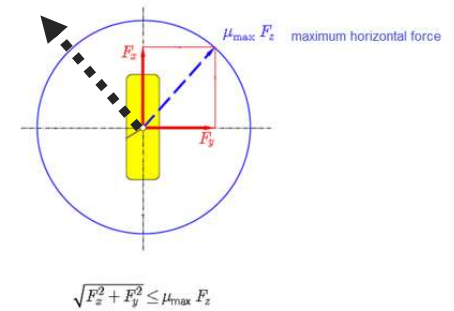


## KIA



### Kamm circle

Circle of friction



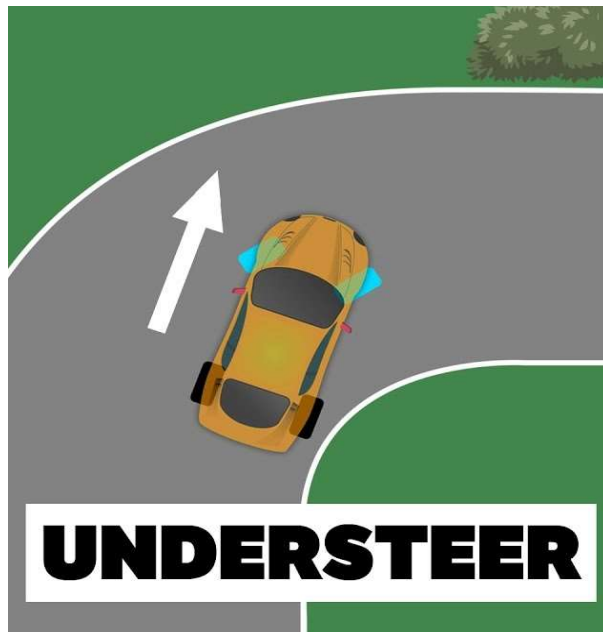


**THE**

## video comments

### Understeer

- predictable
- easier to correct: reduce steering angle, lift off throttle
  - RWD: more throttle
- „Lift off oversteer”
- road cars



### Oversteer

- better because you don't see trees kills you
- reasons: throttle is too big at corner entry / shift down / handbrake
- more difficult to handle



## video comments



video comments



- know concepts and definitions – you are able to give definitions of :
  - different type of tyre radius
  - contact patch
  - tyre structures
  - slip ratio
  - slip angle
  - aware of the different characteristics of tyre behaviour and able to distinguish one from other
  - friction coefficient
  - brush tyre model and explanation of tyre force
  - able to orientate in the coordinate system of a vehicle
  - cornering stiffness of a tyre
  - self aligning torque
  - pneumatic trail
  - friction ,circle'
  - steady state basics equations
  - transient basics equation
  - characteristics of transient basics diagrams

- [https://www.google.com/url?sa=i&url=https%3A%2F%2Fwww.ebay.com%2Fitm%2FTOYOTA-HILUX-Genuine-2012-RHD-ESP-YAW-RATE-SENSOR-89183-60030-1901191-%2F192782917144&psig=AOvVaw3fQLFfTvbjW6tlvt9WA9H2&ust=1614098511238000&source=images&cd=vfe&ved=0CAIQjRxqFwoTCPjyv9T3\\_e4CFQAAAAAdAAAAABAN](https://www.google.com/url?sa=i&url=https%3A%2F%2Fwww.ebay.com%2Fitm%2FTOYOTA-HILUX-Genuine-2012-RHD-ESP-YAW-RATE-SENSOR-89183-60030-1901191-%2F192782917144&psig=AOvVaw3fQLFfTvbjW6tlvt9WA9H2&ust=1614098511238000&source=images&cd=vfe&ved=0CAIQjRxqFwoTCPjyv9T3_e4CFQAAAAAdAAAAABAN)
- Optimum G Seminar by Claude Rouelle 2016 – Graz
- <https://www.youtube.com/watch?v=S0TIRkNWheQ>
- <https://www.sciencedirect.com/science/article/pii/S156849461500650X>

**Thank you for your attention!**

