



1. Subject name **Stochastic Processes in System Dynamics II.**

2. Subject name in Hungarian Sztochasztikus folyamatok a rendszerdinamikában II.

3. Code	BMEKOVJD010	4. Evaluation type	exam grade	5. Credits	4
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6. Weekly contact hours	2 (0) Lecture	0 (0) Practice	0 (0) Lab
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7. Curriculum	PhD Programme	8. Role	Basic course
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9. Working hours for fulfilling the requirements of the subject	120
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Contact hours	28	Preparation for seminars	30	Homework	15
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Reading written materials	15	Midterm preparation	0	Exam preparation	32
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10. Department **Department of Aeronautics and Naval Architectures**

11. Responsible lecturer Dr. Zobory István

12. Lecturers Dr. Zobory István

13. Prerequisites **recommended: BMEKOVJD009 - Stochastic Processes in System Dynamics I.**

14. Description of lectures

Horizontal and vertical treatment of stochastic processes. The fundamental theorem of Kolmogorov. Characteristic functions of stochastic processes. Expected value function, momentum functions and autocorrelation function. The Hilbert-space $L_2(\mathbb{R}, A, P)$. The stochastic process as an "in-space curve" in the Hilbert-space. Some simple stochastic processes. The manifold of straight lines of random position. Stochastic differential equations, two characteristic types. Point processes, counting processes. The three conditions together result in a Poisson-process. Characteristic functions of the Poisson-process. Secondary processes generated by point process. The one-dimensional marginal distribution. The one-dimensional limit-distribution. Renewal processes. Smith-theorem of the renewal theory. Operation process model for machinery systems, generated by a point process. Torque process and RPM process of the driving shaft. Determining the joint limit distribution by using the theorem of complete probability. Some simple variations for point process generated secondary process. Markov-chains and processes. Properties of the transition probability matrices. Marginal distributions of the Markov-chain. Single dimensional random walk on the integers. Stationary Markov-chains. Ergodic Markov-chains. Transition-density functions. The Chapman-Kolmogorov equation. The birth-death process. Model for the service-theory. Permanent distribution. Stationary processes. Strict- and weak stationarity of different order. Spectral properties. Ergodicity with respect to the expected value function and to the autocorrelation function. Gaussian-processes. Basic properties of the Brown-motion process. Characteristic functions of the Brown-motion process.

15. Description of practices

16. Description of laboratory practices

17. Learning outcomes

- A. Knowledge B. Skills
- Students must know comprehensively, interpret in a constructive way and apply in his research activities in an innovative way the following elements of analysis methods: characteristic operations for stochastic processes; methods of application of point processes; procedures for applying Markov-chains; applicability of Markov-chains concerning the solution to mass-service tasks; the analytic properties of stochastic processes.
- C. Attitudes D. Autonomy and Responsibility
- Students must pursue to get knowledge of the new scientific results, the latter are applied with responsibility and initiates new resource activities in new fields of knowledge in an innovative way.

18. Requirements, way to determine a grade (obtain a signature)

Accepted homework sent before the deadline and written exam.

19. Opportunity for repeat/retake and delayed completion

According to the TVSZ

20. Learning materials

1. Zobory, I.: Sztochasztikus folyamatok a rendszerdinamikában I. Kézirat. BME Vasúti Járművek és Járműrendszeranalízis Tanszék. Budapest, 2011.

2. Arnold, L.: Sztochasztikus differenciálegyenletek Tipotex, Budapest, 2013.

Effective date

27 November 2019

This Subject Datasheet is valid for

Inactive courses
